

* Task 1: Cartesian Curves

Trace the following curve.

$$2 \quad xy^2 = a^2(a-x)$$

Given eqⁿ of curve is $xy^2 = a^2(a-x)$

1 Symmetry:

In given eqⁿ of curve we replacing y by $-y$ and eqⁿ remain unchanged then curve has symmetry about x axis.

2 Curve passing through the origin.

In eqⁿ of curve we can see a constant then curve does not pass through the origin.

3 Intersection with axis.

In eqⁿ of curve we putting $y=0$ then we get co-ordinate point of intersection with x axis.

$$\therefore xy^2 = a^2(a-x)$$

$$\therefore 0 = a^3 - a^2x$$

$$\therefore \boxed{x = a}$$

4 Asymptotes

① parallel to x axis:

$$\therefore xy^2 = a^3 - a^2x$$

$$\therefore xy^2 + a^2x = a^3$$

$$\therefore x = \frac{a^3}{y^2 + a^2}$$

$$\therefore y^2 + a^2 = 0$$

$$\therefore y = \pm \sqrt{-a}$$

② parallel to y axis

$$\therefore xy^2 = a^3 - a^2x$$

$$\therefore \boxed{x = 0}$$

5 Region, For region Form the curve eqⁿ

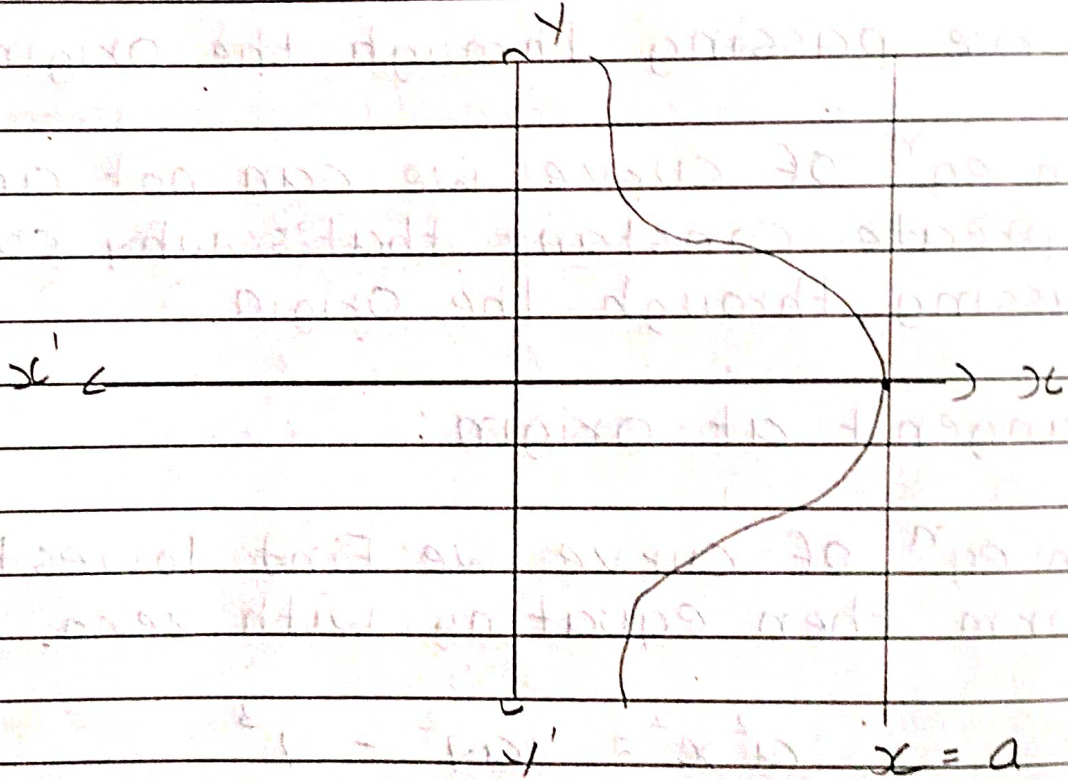
$$\therefore xy^2 = a^2(a-x)$$

$$\therefore y^2 = \frac{a^2(a-x)}{x}$$

$$\therefore y = a \sqrt{\frac{a-x}{x}}$$

Here, y become imaginary For $x > a$, $x \leq 0$.

So, Curve does not lies for $x > a$ and $x \leq 0$.



$$3 \quad a^2 x^2 = y^2(2a - y)$$

Given eqⁿ of curve $a^2 x^2 = y^2(2a - y)$ - (1)

1 Symmetry:

In eqⁿ of curve we replacing x by $-x$ eqⁿ of curve remain unchange then curve has symmetry above y -axis.

2 Curve passing Through the origin

In eqⁿ of curve we can not any seprate constant that's why curve passing through the origin.

3 Tangent at origin:

In eqⁿ of curve we Find lowest degree term then equating with zero.

$$a^2 x^2 = 2ay^2 - y^3$$

$$\therefore a^2 x^2 - 2ay^2 = 0$$

$$\therefore a^2 x^2 = 2ay^2$$

$$\therefore ax^2 = 2y^2$$

$$\therefore \pm \sqrt{ax} = \pm \sqrt{2y}$$

$$\text{So, } \sqrt{ax} - \sqrt{2y} = 0, \quad -\sqrt{ax} - \sqrt{2y} = 0$$

$$\sqrt{ax} + \sqrt{2y} = 0, \quad -\sqrt{ax} + \sqrt{2y} = 0$$

$\therefore \sqrt{ax} - \sqrt{2y} = 0$ and $\sqrt{ax} + \sqrt{2y}$ is tangent at origin.

Here, we get 2 tangent at Origin but tangent is not equal. So, Origin is a become Node.

4 Intersection with axis

① For X axis : We take $Y = 0$ In eqⁿ of curve.

$$\therefore a^2 x^2 = y^2 (2a - y)$$

$$\therefore a^2 x^2 = 0$$

$$\therefore x = 0$$

② For Y axis : We take $X = 0$ in eqⁿ of curve.

$$\therefore a^2 x^2 = y^2 (2a - y)$$

$$y^2 (2a - y) = 0$$

$$\therefore y^2 2a = y^3$$

$$\therefore y = 2a$$

Curve intersection with X axis at $x = 0$ and Y axis at $y = 2a$ point.

5 Region.

$$\therefore a^2 x^2 = y^2 (2a - y)$$

$$\therefore a^2 x^2 = y^2 2a - y^3$$

$$\therefore x^2 = \frac{y^2 2a - y^3}{a^2}$$

$$\therefore x = \frac{y \sqrt{2a - y}}{a}$$

Here, x become imaginary for $y > 2a$.
So, Curve does not lies for $y > 2a$.

6 Asymptotes.

① parallel to x axis:

In eqⁿ of curve equate highest degree x coefficient with zero

$$\therefore x^2 a^2 = 0$$

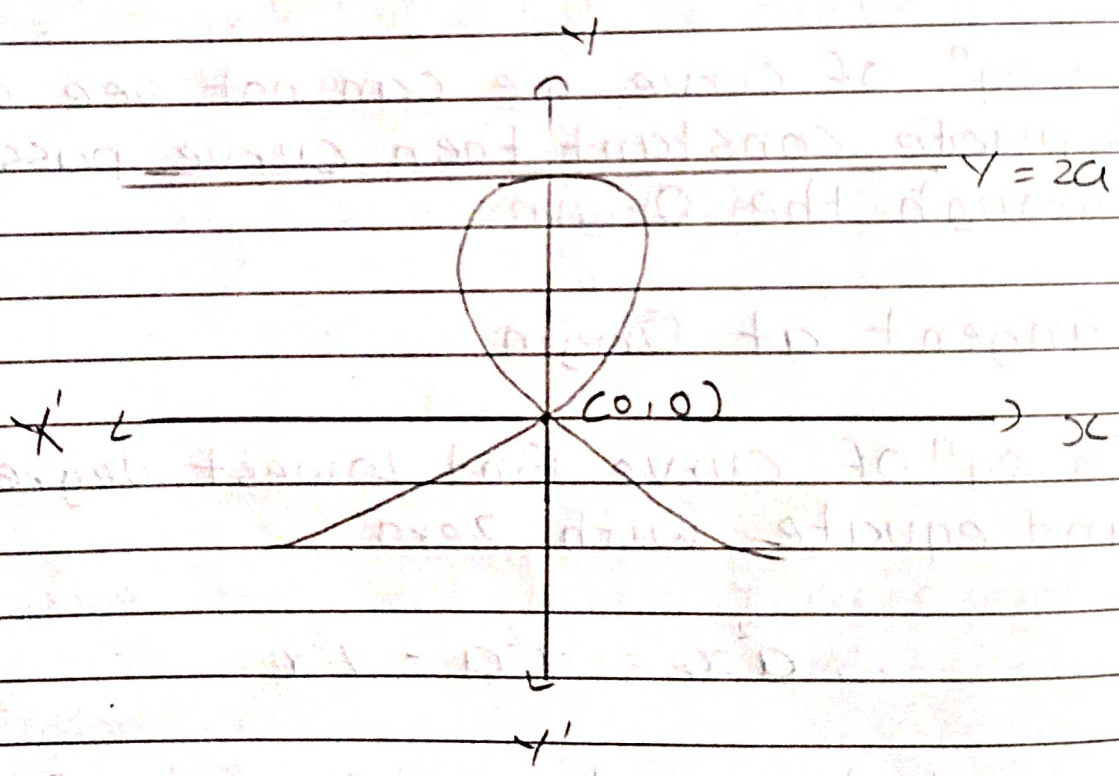
$$\therefore a^2 = 0$$

② parallel to Y axis :

In eqⁿ of curve equate highest degree Y coefficient with zero.

$$\therefore -y^3 = -1$$
$$\text{So, } -1 \neq 0$$

Asymptotes is does not exist at parallel to Y axis and X axis.



$$4 \quad ay^2 = a^2x = y^2(ca-x)$$

Given eqⁿ of curve $a^2x = y^2(ca-x)$ - (1)

1 Symmetry:

In eqⁿ of curve we replacing y by $-y$ then eqⁿ of curve remain unchange then curve has symmetry above x axis.

2 Curve passing through the Origin.

In eqⁿ of curve we can not see any separate constant then curve passing through the Origin.

3 Tangent at Origin.

In eqⁿ of curve Find lowest degree term and equate with zero.

$$\therefore a^2x = y^2a - y^2x$$

Lowest degree term is $a^2x = 0$

$$\therefore x = 0$$

4 Intersection with axis,

① For X axis: In eqⁿ of curve we take
 $y = 0$

$$\therefore a^2 x = y^2 (a - x)$$

$$\therefore x = 0$$

Curve intersect with x axis at Origin

② For Y axis: In eqⁿ of curve we take
 $x = 0$

$$\therefore a^2 x = y^2 (a - x)$$

$$\therefore y^2 a = 0$$

$$\therefore y = 0$$

Curve intersect with Y axis at Origin

5 Region:

$$\therefore a^2 x = y^2 (a - x)$$

$$\therefore y^2 = \frac{a^2 x}{a - x}$$

$$\therefore y = a \sqrt{\frac{x}{a - x}}$$

y become imaginary For $x = a$, $x > a$, $x < 0$.

6 Asymptotes :-

1 parallel to x axis:

In eqⁿ of curve equate highest degree x coefficient with zero.

$$a^2 x = y^2 a - y^2 x$$

$$\therefore a^2 x + y^2 x = y^2 a$$

$$\therefore x = \frac{y^2 a}{a^2 + y^2}$$

$$\therefore a^2 + y^2 = 0$$

$$\therefore y = \pm \sqrt{-a^2}$$

2 parallel to y axis:

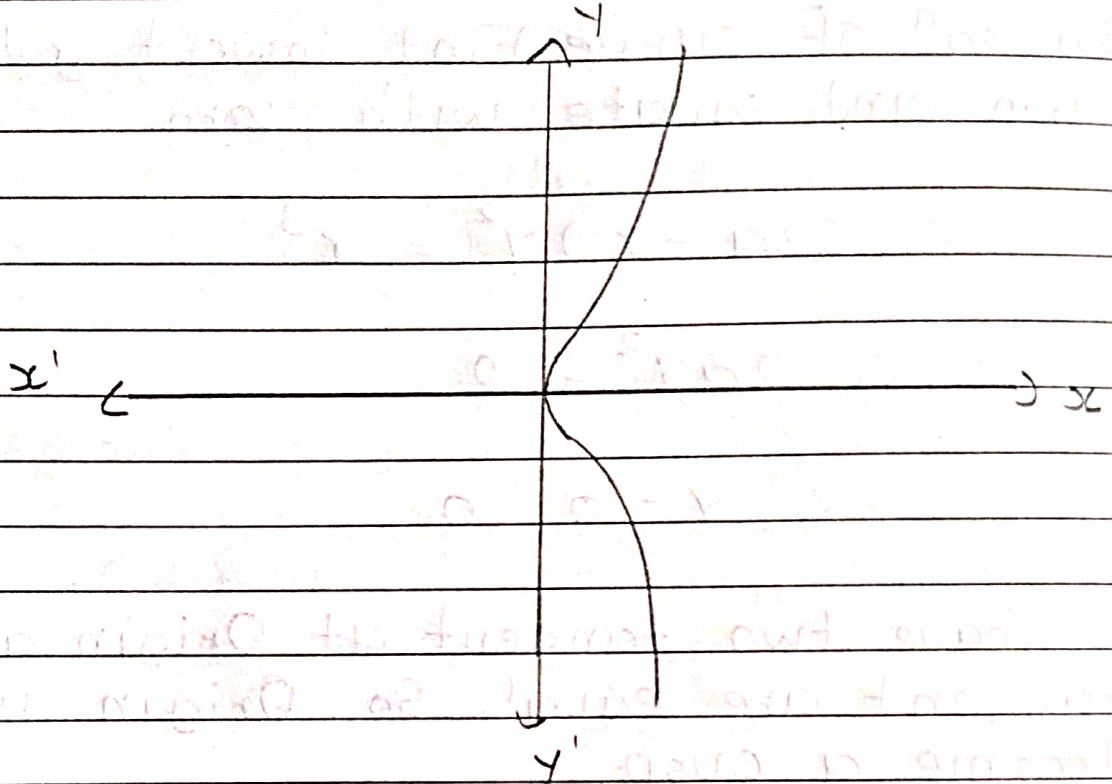
In eqⁿ of curve equate Highest degree y coefficient with zero.

$$a^2 x = y^2 (a - x)$$

$$\therefore a - x = 0$$

$$\therefore x = a$$

Asymptotes is not exist at parallel to X axis. It is exist at parallel to Y axis.



$$1 \quad (2a-x)y^2 = x^3$$

Given eqⁿ of curve $(2a-x)y^2 = x^3$ - (1)

1 Symmetry:

In given eqⁿ of curve we replacing y by $-y$ then eqⁿ remain unchange. So, Curve has Symmetry above X axis.

2 Tangent at Origin:

In given eqⁿ of curve we can see that any constant term is not separate.

in eqⁿ. So, Curve has tangent at origin.

3 Tangent at Origin

In eqⁿ of curve Find lowest degree term and equate with zero.

$$\therefore (2a - x)y^2 = x^3$$

$$\therefore 2ay^2 = 0$$

$$\therefore y = 0, 0$$

We have two tangent at Origin and tangent are equal. So, Origin is become a cusp.

4 Intersection with axis

① For X axis: In eqⁿ of curve putting $y=0$

$$\therefore (2a - x)y^2 = x^3$$

$$\therefore x^3 = 0$$

$$\therefore x = 0$$

② For Y axis: In eqⁿ of curve putting $x=0$.

$$\therefore (2a-x)y^2 = x^3$$

$$\therefore 2ay^2 = 0$$

$$\therefore y = 0$$

Intersection with axis Curve has
Intersect with y and x axis at
Origin.

5 Region:

$$(2a-x)y^2 = x^3$$

$$\therefore y^2 = \frac{x^3}{2a-x}$$

$$\therefore y = x \sqrt{\frac{x}{2a-x}}$$

y become imaginary for $x > 2a$.

6 Asymptotes:

① parallel to x axis: In eqⁿ of curve
equate highest degree x coefficient
with x 0

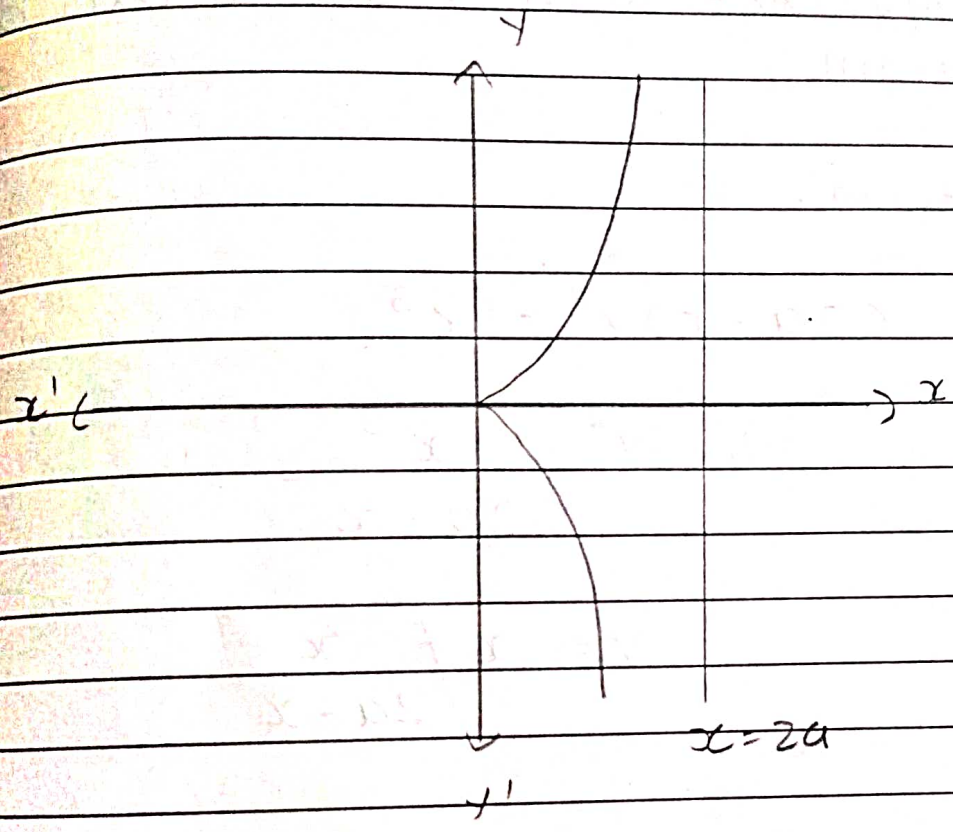
$$\therefore x^3 = 0$$

$$\therefore x = 0$$

parallel to Y axis : In eqⁿ of curve equate highest degree Y coefficient with 0

∴ 2a - x = 0

∴ x = 2a



5 $9ay^2 = x(x - 3a)^2$

Given eqⁿ of Curve $9ay^2 = x(x - 3a)^2$ - (1)

1 Symmetry : In given eqⁿ of curve we replasing y by -y then eqⁿ of curve remain unchange.

So, Curve has symmetry above X axis.

2 Curve passing through the Origin.

In eqⁿ of curve we can see that any constant term does not separate In eqⁿ. So, Curve passing through the Origin.

3 Tangent at Origin:

In eqⁿ of curve Find lowest degree term and equate with zero.

$$\therefore gay^2 = x(x^2 - 6xa + 9a^2)$$

$$\therefore gay^2 - x^3 + 6x^2a - 9a^2x = 0$$

here, lowest degree term

$$\therefore -9a^2x = 0$$

$$\therefore x = 0$$

Curve has tangent at Origin.

4 ~~Intersection with axis~~ Asymptotes

① For X axis: In eqⁿ of curve equate highest degree X coefficient with zero.

$$\therefore x^3 = 0$$

$$x = 0$$

② For y axis: In eqⁿ of curve equate highest y coefficient with 0

$$\therefore -9ay^2 = 0$$

$$\therefore y = 0$$

Asymptotes is exist \emptyset for X and Y axis.

5 Intersection with axes.

① For X axis: In eqⁿ of curve putting $y = 0$

$$\therefore x(x-3a)^2 = 0$$

$$\therefore x = 3a$$

② For Y axis: In eqⁿ of curve putting $x = 0$

$$9ay^2 = 0$$

$$y = 0$$

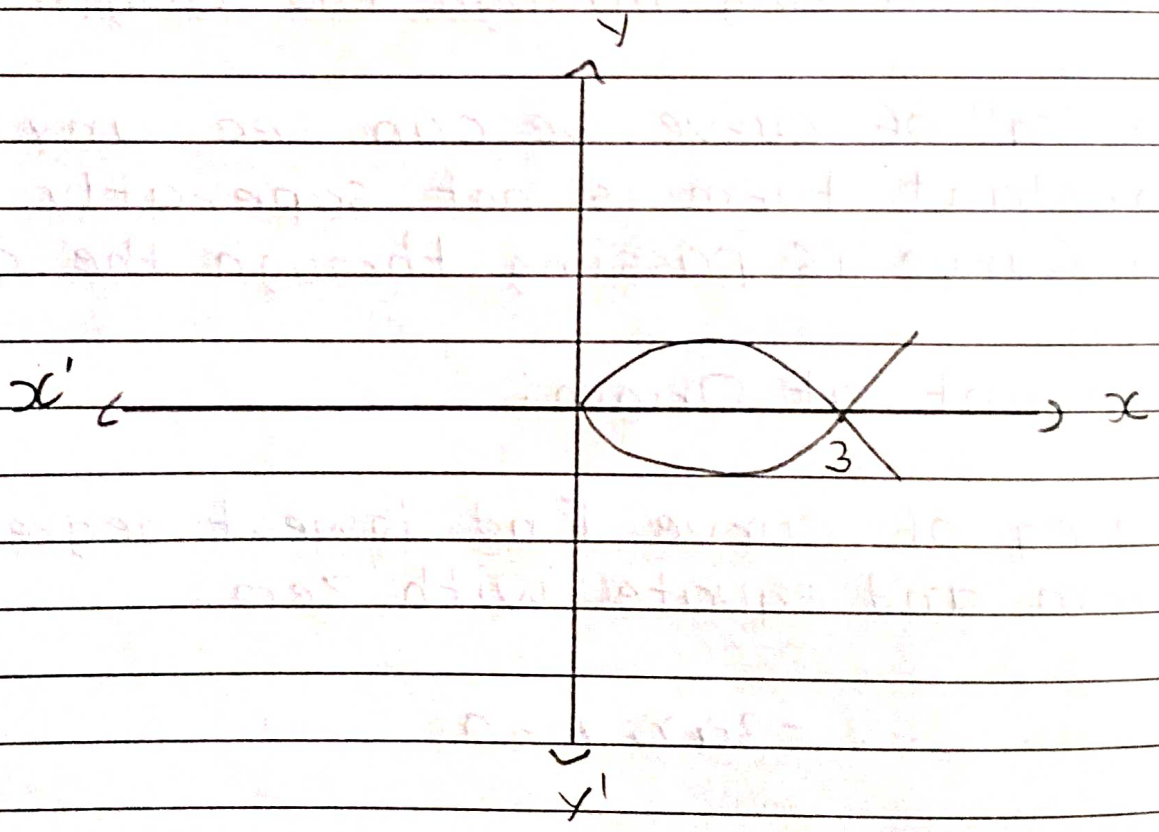
6 Region :

$$y^2 = \frac{x(x-3a)^2}{9a}$$

$$\therefore y = \frac{(x-3a)}{3} \sqrt{\frac{x}{a}}$$

$$0 \leq x \leq 3a$$

y become imaginary for $0 \leq x < 3a$.



$$6 \quad x^3 + y^3 - 3axy = 0$$

Given eqⁿ of curve $x^3 + y^3 - 3axy = 0$ — (1)

1 Symmetry: In the given eqⁿ of curve, if we interchange x and y eqⁿ of curve remain unchange.

So, curve is symmetry above $x = y$ line.

2 Curve passing through the Origin:

In eqⁿ of curve we can see any constant term is not separately.

So, Curve is passing through the Origin.

3 Tangent at Origin:

In eq of curve Find lowest degree term and equate with zero.

$$\therefore -3axy = 0$$

$$\therefore x = 0, y = 0$$

At Origin we get 2 different tangent.
So, Origin is become a node point.

4 Intersection with axis.

Intersection For $Y = X$ line,
take $x = Y$ in eqⁿ 1

$$\therefore x^3 + x^3 = 3ax^2$$

$$\therefore x = \frac{3a}{2}, \quad Y = \frac{3a}{2}$$

So, Curve into the $Y = X$ line at $\left(\frac{3a}{2}, \frac{3a}{2}\right)$

5 Region.

If we take $X = (C - X)$ and $Y = (C - Y)$

So, Curve does not go in 3rd quadrant.

6 Asymptotes:

(i) Parallel to X axis = No

(ii) Parallel to Y axis = No

(iii) Oblique Asymptotes: $Y = mx + c$

Now, For Asymptotes, we take

$$\phi_n(m) = \phi_3(m) = 1 + m^3$$

$$\therefore \phi_{n-1}(m) = \phi_2(m) = -3am$$

Now, we take $\phi_n(m) = 0$

$$\therefore 1 + m^3 = 0$$

$$\therefore (m+1)(m^2 - m + 1) = 0$$

$m^2 - m + 1 = 0$ has imaginary root.

$$\text{So, } m+1 = 0, \quad m = -1$$

Now C Find as Follow

$$C = \frac{-\phi_{n-1}(m)}{\phi'_n(m)} = \frac{-(-3am)}{3m^2}$$

$$\therefore C = \frac{a}{m}$$

$$\therefore C = -a$$

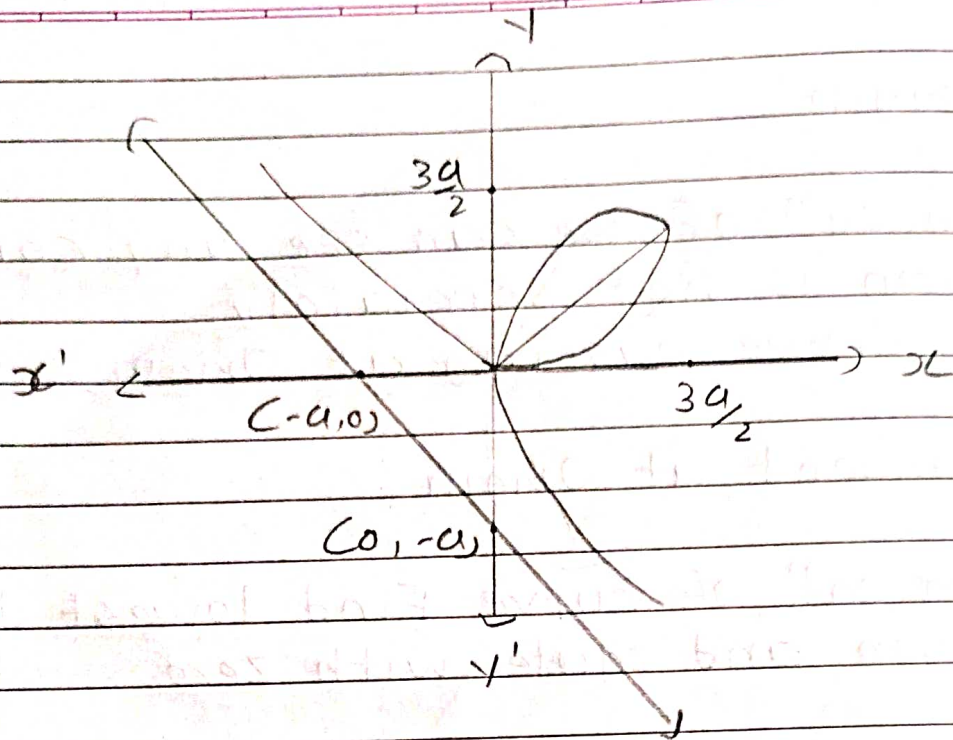
Now oblique Asymptotes

$$\therefore y = mx + c$$

$$\therefore y = -m - a$$

$$\therefore x + y = -a$$

$$\therefore (0, -a), (a, 0)$$



$$7 \quad y^2(a^2 + x^2) = x^2(a^2 - x^2)$$

Given eqⁿ of curve $y^2 a^2 + y^2 x^2 = x^2 a^2 - x^4$

1 Symmetry:

- In eqⁿ of curve remains unchange when replasing x by $-x$. So the curve is Symmetry above Y axis.
- In eqⁿ of curve remains unchange when replasing x by $-x$ and y by $-y$. So the curve has symmetry above opposite quadrant.
- In eqⁿ of curve remains unchange when replasing y by $-y$. So the curve has symmetry above X axis.

Origin:

In eqⁿ of we can see any constant term is not separately.
So, Curve passing at Origin.

Tangent at Origin:

In eqⁿ of curve Find lowest degree term and equate with zero.

lowest degree term is $y^2 a^2 = 0$
 $x^2 a^2 = 0$

$\therefore x = 0, y = 0$

two tangent are different So, Origin become a node.

4 Intersection with axis:

① For X axis: In eqⁿ of curve putting $y = 0$

$\therefore x^2 a^2 = x^4$

$\therefore x = a$

② For Y axis: In eqⁿ of curve putting $x = 0$

$$\therefore y^2 a^2 = 0$$

$$\therefore y = 0$$

5 Region:

$$y^2 = \frac{x^2 (a^2 - x^2)}{a^2 + x^2} \rightarrow y = x \sqrt{\frac{a^2 - x^2}{a^2 + x^2}}$$

$$x^2 = \frac{y^2 (a^2 + x^2)}{a^2 - x^2} \rightarrow x = y \sqrt{\frac{a^2 + x^2}{a^2 - x^2}}$$

$$-a \leq x \leq a$$

6 Asymptotes:

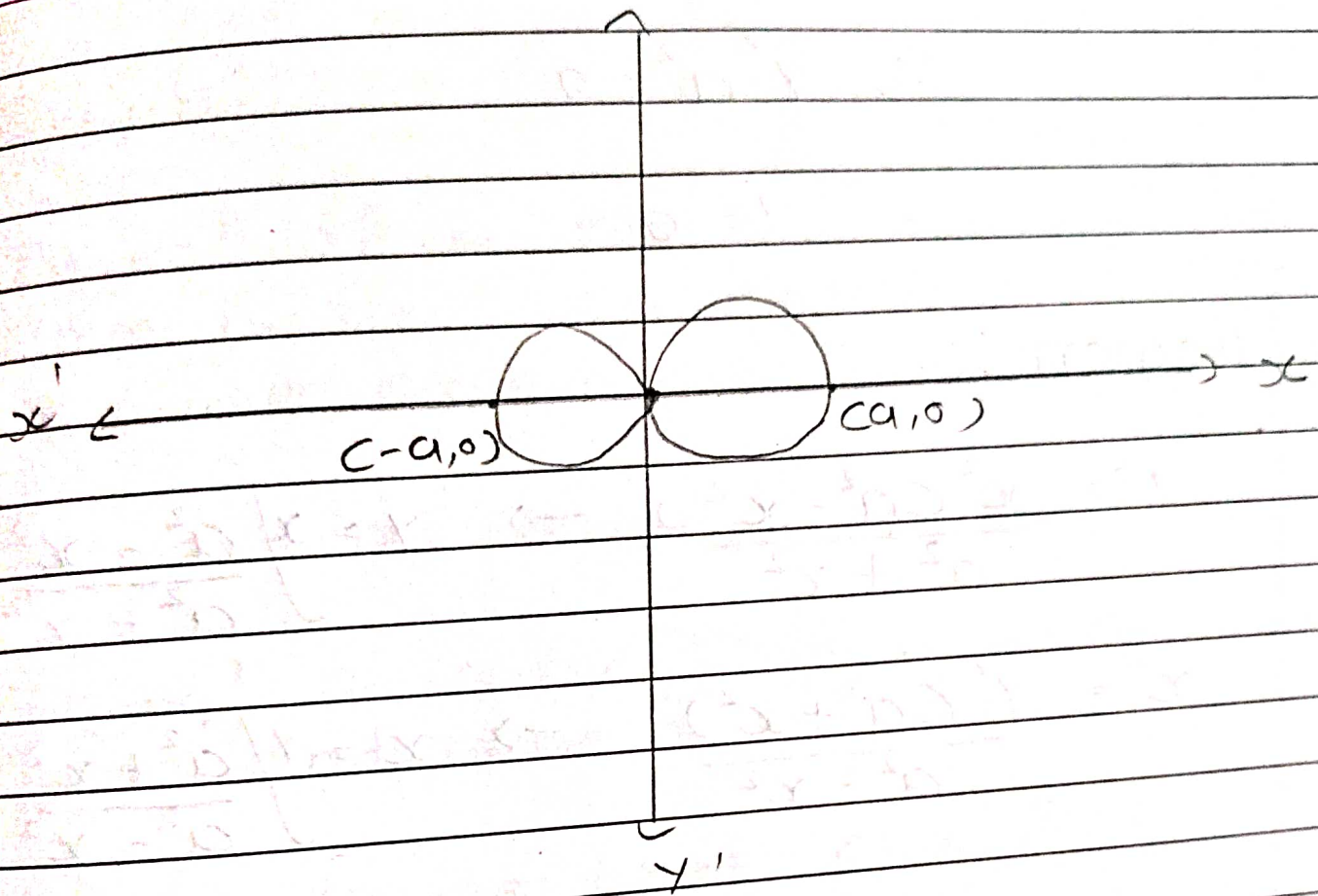
(i) Parallel to x axis: No

(ii) Parallel to y axis: No

(iii) Oblique Asymptotes: $y = mx + c$

$$\phi_n(m) = \phi_2(m) = m^2 - 1$$

$$\therefore \phi_{n-1}(m) = \phi_1(m) =$$



Unit-3 Curve Tracing

* Task 2: Polar curves

1 $r = a(1 - \cos\theta)$

Here given eqⁿ of the curve is $r = a(1 - \cos\theta)$.
We want to trace the curve by following steps.

1 Symmetry:

In eqⁿ of curve remains unchanged by replacing θ by $-\theta$. That's why curve has initial line symmetry.

2 Passing through the Pole:

When we take $r=0$ and eqⁿ give such θ then curve passing through the pole.

$$\therefore r = a(1 - \cos\theta)$$

$$\therefore a(1 - \cos\theta) = 0$$

$$\therefore 1 - \cos\theta = 0$$

$$\therefore \cos\theta = 1$$

$$\therefore \theta = 0$$

Here, we have such value of θ that's why curve passing through the pole.

3 Tangent at Pole:

We take $r=0$ and we get $\theta=0$ then curve has tangent at Pole.

4 Direction of tangent:

Direction of tangent we find by formula,

$$\tan \phi = \frac{r}{dr/d\theta}$$

$$= \frac{a(1 - \cos\theta)}{a \sin\theta}$$

$$= \frac{1 - \cos\theta}{\sin\theta}$$

$$= \frac{2 \sin^2 \theta/2}{2 \sin\theta/2 \cdot \cos\theta/2}$$

$$= \frac{2 \sin^2 \theta/2}{2 \sin\theta/2 \cdot \cos\theta/2}$$

$$\tan \phi = \tan \frac{\theta}{2}$$

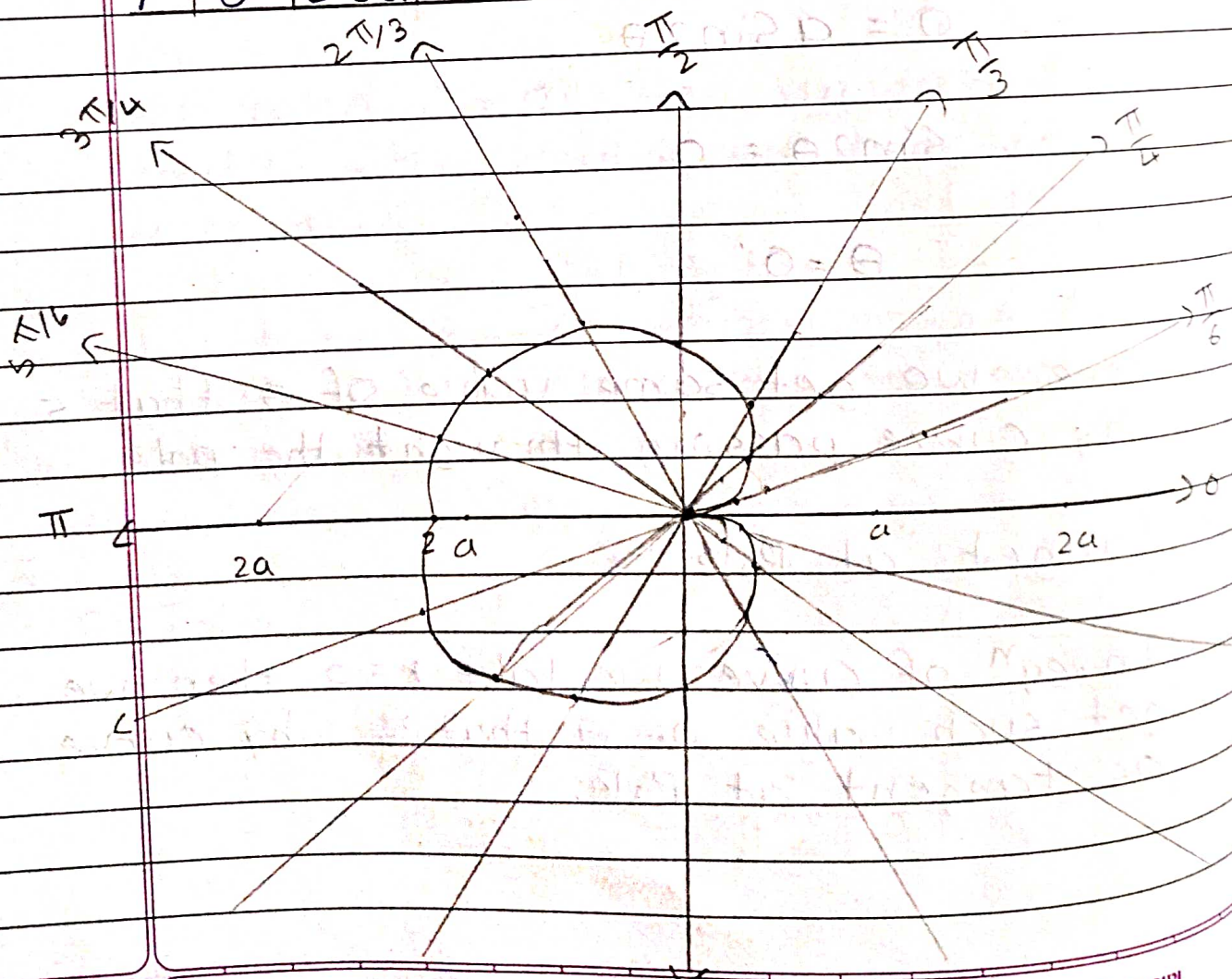
$$\therefore \phi = \frac{\theta}{2}$$

We take $\theta = 0^\circ$ then $\phi = 0$, So radius and tangent vector are equal

We take $\theta = \pi$ then $\phi = \pi/2$, So radius and tangent vector are perpendicular

5 table.

θ	0	$\frac{\pi}{6}$	$\frac{\pi}{4}$	$\frac{\pi}{3}$	$\frac{\pi}{2}$	$\frac{2\pi}{3}$	$\frac{3\pi}{4}$	$\frac{5\pi}{6}$	π
r	0	0.3a	0.29a	0.5a	a	1.5a	1.7a	1.86a	2a



2 $r = a \sin 2\theta$

1 Symmetry :

In eqⁿ of Curve we change θ by $-\theta$ then eqⁿ of Curve remain unchange that's why curve as symmetry above initial line.

2 Passing through the pole :-

In eqⁿ of Curve we take $r=0$ then we get such θ value.

$$\therefore 0 = a \sin 2\theta$$

$$\therefore \sin 2\theta = 0$$

$$\therefore \theta = 0$$

Here, we get same value of θ that's why curve passing through the pole.

3 Tangent at Pole :

In eqⁿ of curve we take $r=0$ then we get such value of θ that's why curve as tangent at Pole.

4 Direction of tangent

Direction of tangent we find by this formula.

$$\tan \phi = \frac{r}{dr/d\theta}$$

$$= \frac{a \sin 2\theta}{2a \cos 2\theta}$$

$$\tan \phi = \frac{1}{2} \tan 2\theta$$

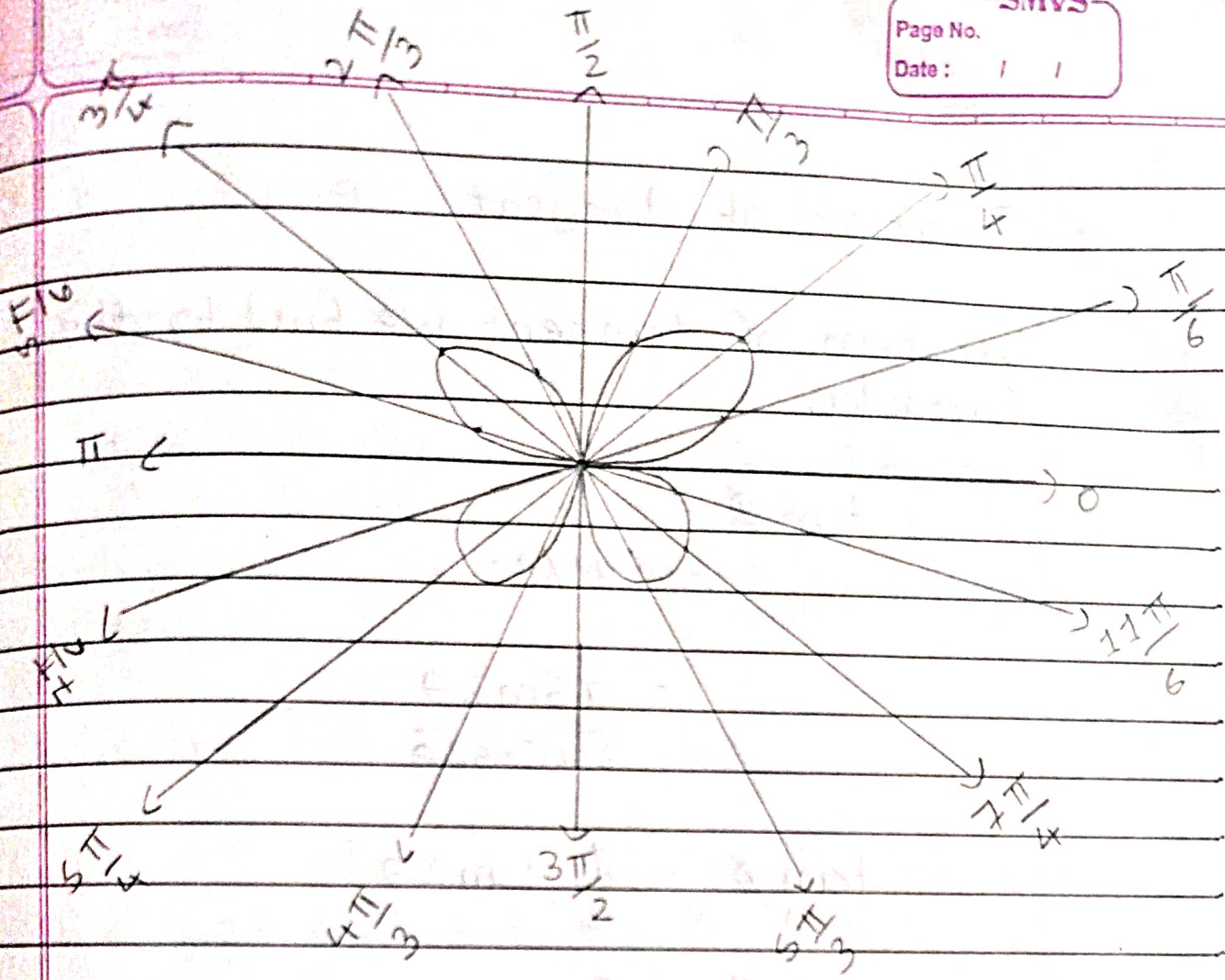
$$\phi = \theta$$

We take $\theta = 0$ then we get $\phi = 0$ that's why radius and tangent vector are equal.

We take $\theta = \pi/2$ then we get $\phi = \pi/2$ that's why radius and tangent vector are perpendicular.

5 Table:

θ	0	$\frac{\pi}{6}$	$\frac{\pi}{4}$	$\frac{\pi}{3}$	$\frac{\pi}{2}$	$\frac{2\pi}{3}$	$\frac{3\pi}{4}$	$\frac{5\pi}{6}$	π
r	0	$\frac{0.86}{a}$	$1a$	$\frac{0.86}{a}$	0	$-\frac{0.86}{a}$	$-1a$	$-\frac{0.86}{a}$	0



3 $r^2 = a^2 \cos 2\theta$

1 Symmetry: In given eqⁿ of we replasing θ by $-\theta$ then eqⁿ of curve remain unchange then curve has symmetry above intal line

If eqⁿ of curve we replasing r by $-r$ and θ by $-\theta$ then eqⁿ of curve remain unchange that's why curve has symmetry above $\pi/2$ line.

2 Passing through the pole:

In eqⁿ of Curve we take $r=0$ then we get such value of θ

$$\therefore r^2 = a^2 \cos 2\theta$$

$$\therefore a^2 \cos 2\theta = 0$$

$$\therefore \cos 2\theta = 0$$

$$\therefore \theta = \frac{\pi}{2}$$

We get such value of θ that's why curve passing through the pole.

3 Tangent at Pole:

We take $r=0$ then we get such value of θ that's why curve has tangent at Pole.

4 Direction of tangent:

Find Direction of tangent use by this formula.

$$r = a \sqrt{\cos 2\theta}, \quad \frac{dr}{d\theta} = \frac{-a \cdot 2 \sqrt{\cos 2\theta} \cdot \sqrt{\sin 2\theta}}{2 \sqrt{\cos 2\theta}}$$

$$= -a \sqrt{\sin 2\theta}$$

$$\therefore \tan \phi = \frac{r}{dr/d\theta} = \frac{a \sqrt{\cos 2\theta}}{-a \sqrt{\sin 2\theta}}$$

$\therefore \tan \theta = -\cot 2\theta$

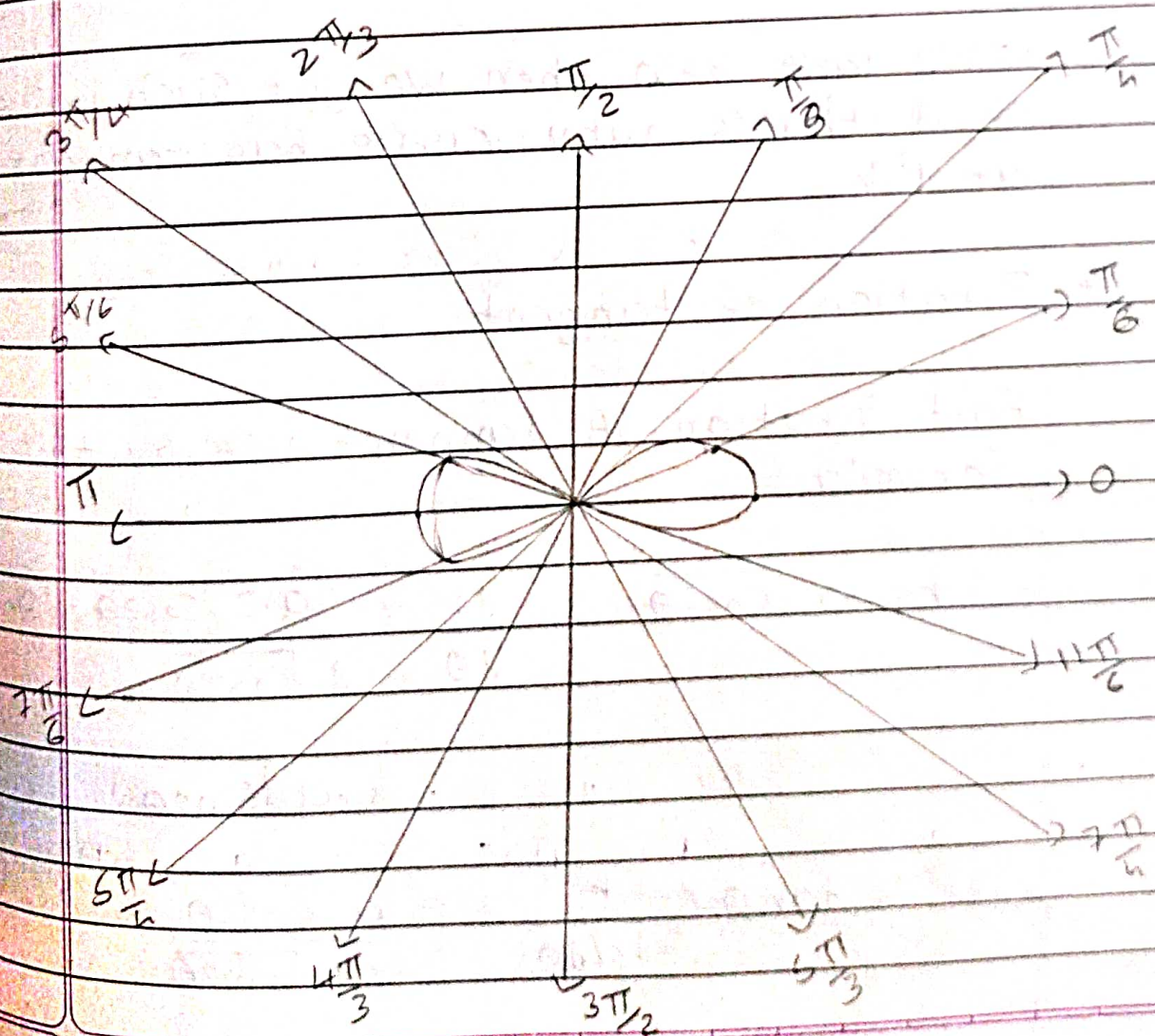
5 Region: Here given eqⁿ curve $r^2 = a^2 \cos 2\theta$ and we know that $\cos \theta$ +ve in 1st and 4th quadrant.

Now, $-\frac{\pi}{2} \leq 2\theta \leq \frac{\pi}{2}$

$\therefore -\frac{\pi}{4} \leq \theta \leq \frac{\pi}{4}$

6 table:

θ	0	$\pi/6$	$\pi/4$	$3\pi/4$	$5\pi/6$	π
r	a	0.7a	0	0	0.7a	a



4 $r = a \sin 3\theta$

1 Symmetry :

In eqⁿ of curve we replasing θ by $-\theta$ then eqⁿ of curve remain unchange that's why curve has symmetry above initial line.

In eqⁿ of Curve we replasing θ by $\pi - \theta$ then eqⁿ of curve remain unchange that's why curve has symmetry above $\pi/2$ line.

2 Passing through the Pole

We take $r=0$ then we get such value of θ

$$\therefore r = a \sin 3\theta$$

$$\therefore a \sin 3\theta = 0$$

$$\therefore \theta = 0$$

3 To Here, we get such value of θ then curve has passing through the pole.

3. Tangent at Pole:

We take $r=0$ then we get such value of $\theta=0$ that's why curve as tangent at Pole.

4. Direction of tangent:

We Find Direction of tangent by use this formula.

$$\begin{aligned} \tan \phi &= \frac{r}{dr/d\theta} \\ &= \frac{a \sin 3\theta}{3a \cos 3\theta} \end{aligned}$$

$$\therefore \tan \phi = \frac{1}{3} \tan 3\theta$$

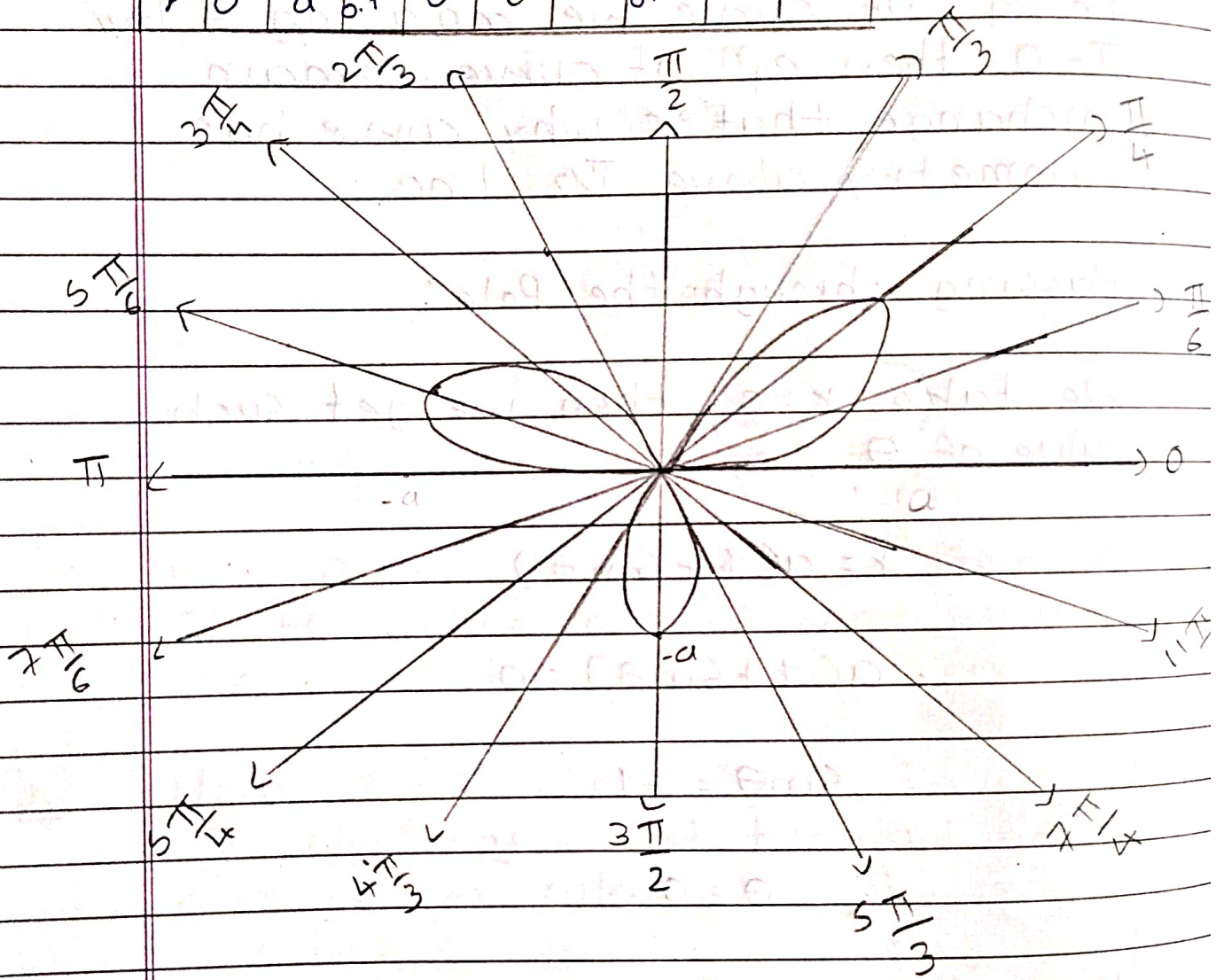
$$\therefore \phi = \theta$$

We take $\phi=0$ then $\theta=0$. So, radius and tangent vector are perpendicular equal.

We take $\phi=\pi/2$ then $\theta=\pi/2$. So, radius and tangent vector are perpendicular.

5 Table:

θ	0	$\frac{\pi}{6}$	$\frac{\pi}{4}$	$\frac{\pi}{3}$	$\frac{\pi}{2}$	$\frac{2\pi}{3}$	$\frac{3\pi}{4}$	$\frac{5\pi}{6}$	π
r	0	a	0.7^a	0	-a	-a	0.7^a	a	0



$$5 \quad r = a(1 + \sin\theta)$$

1 Symmetry:

In eqⁿ of curve we replacing θ by $\pi - \theta$ then eqⁿ of curve remain unchange that's why curve has symmetry above $\pi/2$ line.

2 Passing through the Pole:

We take $r=0$ then we get such value of θ

$$\therefore r = a(1 + \sin\theta)$$

$$\therefore a(1 + \sin\theta) = 0$$

$$\therefore \sin\theta = -1$$

$$\therefore \theta = \pi$$

Here, such θ value are exist that's why curve passing through the Pole.

3 Tangent at Pole:

We take $r=0$ and we get such value of $\theta = \pi$ so, curve has tangent at Pole.

4 Direction of tangent

Direction of tangent we find by this formula,

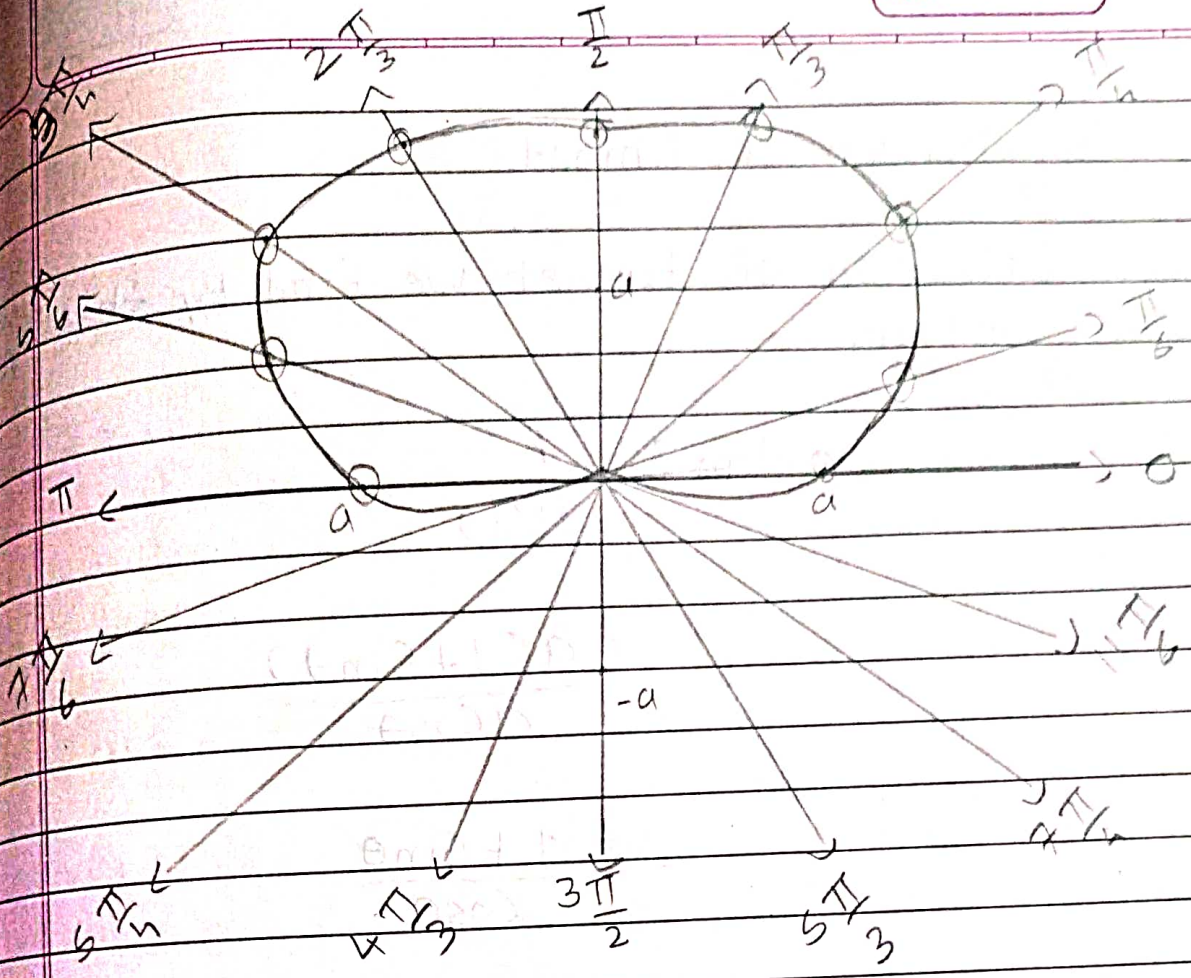
$$\begin{aligned} \therefore \tan \phi &= \frac{r}{dr/d\theta} \\ &= \frac{a(1 + \sin\theta)}{a \cos\theta} \\ &= \frac{1 + \sin\theta}{\cos\theta} \end{aligned}$$

Here, $\theta \rightarrow 0$, then $\tan \phi = 0$, then $\phi = 0$
So, the radius and tangent vector are equal.

Here, $\theta \rightarrow \pi$ then $\phi = \pi/2$.
So, the radius and tangent vector are perpendicular.

5 Table:

θ	0	$\frac{\pi}{6}$	$\frac{\pi}{4}$	$\frac{\pi}{3}$	$\frac{\pi}{2}$	$\frac{2\pi}{3}$	$\frac{3\pi}{4}$	$\frac{5\pi}{6}$	π
r	a	1.5a	1.7a	1.86a	2a	1.86a	1.7a	1.5a	a



6 $r = a \cos 2\theta$

1 Symmetry :

In given eqⁿ of curve we replasing θ by $-\theta$ eqⁿ of curve remain unchange then curve has symmetry above initial line.

2 Passing through the Pole :

given eqⁿ of curve we take $r=0$ then we get such value of θ

$$\therefore r = a \cos 2\theta$$

$$\therefore a \cos 2\theta = 0$$

$$\therefore 2\theta = \pi$$

$$\therefore \theta = \frac{\pi}{2}$$

Here, we get $\theta = \pi/2$ then eqⁿ of curve passing through the Pole.

3 Tangent at Pole:

We take $r = 0$ then we get $\theta = \pi/2$.
So, curve has tangent at Pole.

4 Direction of tangent

Direction of tangent we find use of this formula,

$$\tan \phi = \frac{r}{\partial r / \partial \theta}$$

$$= \frac{a \cos 2\theta}{-2a \sin 2\theta}$$

$$= -\frac{1}{2} \cot 2\theta$$

Here, we take $\theta = \pi/2$ then $\phi = 0$.
So, radius and tangent vector are equal.

We take $\theta = 0$ then $\phi = \pi/2$
So, radius and tangent vector are perpendicular.

Table

θ	0	$\frac{\pi}{6}$	$\frac{\pi}{4}$	$\frac{\pi}{3}$	$\frac{\pi}{2}$	$\frac{2\pi}{3}$	$\frac{3\pi}{4}$	$\frac{5\pi}{6}$	π
r	$1a$	$0.5a$	0	$-0.5a$	$-0.6a$	$-0.8a$	$-0.9a$	$-1a$	$1a$

