

* Context-Sensitive Grammar:

=> Context-Sensitive Grammar is a Type-1 Grammar

This Grammar is recognized by Linear Bound Automata.

Type-1 Grammar is only contains transformation of symbol which is α and β

A Context-Sensitive Grammar is an Unrestricted Grammar.

In this Grammar α and β are strings of non-terminals and terminals.

$$\alpha \rightarrow \beta$$

Where $\alpha, \beta \in (V \cup T)^+$ and $|\alpha| \leq |\beta|$

Context-Sensitive Grammars are more powerful than Context-Free Grammars.

* Linear Bounded Automata:

=> Linear Bounded Automata is used to recognized Context-Sensitive Grammar.

LBA can be defined with Eight Tuples.

$$M = \{Q, T, E, q_0, M_L, M_R, S, F\}$$

where,

Q -> Finite set of states

T -> Tape Alphabet

E -> Input Symbol

q_0 -> Initial state

M_L -> Left Bound of tape

M_R -> Right Bound of tape

S -> Transition Function

F -> Final states



* Pumping Lemma:

\Rightarrow Pumping Lemma is used to prove that a language is NOT Regular.

IF A is a Regular Language then A has a Pumping Length P such that any string S may be divided into 3 Parts $S = XYZ$

This are the Condition:

- (i) $XYZ \in A$ for every $i \geq 0$
- (ii) $|Y| > 0$
- (iii) $|XY| \leq P$

IF this Three condition is True then This Language is Regular Language else NOT Regular Language.

Ex. Prove that Language $A = \{a^n b^n \mid n \geq 0\}$ is NOT Regular.

\Rightarrow Assume that, Here A is a Regular Language and Pumping Length $P = 7$

$$\therefore S = a^7 b^7 = aaaaaaaabbbbbbb$$

We have to Divide This S String into three parts.

So, $X = aaaaaa$
 $Y = aab$
 $Z = bbbbbb$

We have to check Three Pumping Lemma Condition.

(i) $XYZ \in A$

Here, XYZ is always belongs to the part of the A Regular Language.

(ii) $|Y| > 0$

Here, we have to take Y' and check with S string

Here, we take $Y = Z$

$\therefore XY^2Z = aaaaaaabaab$
 $bbbbbb$

$\therefore XYZ = aaaaaaabbbbb$

Here, $XY^2Z \neq XYZ$

(iii) $|X|$
 $|Y|$
 $|Z|$

Ex F
 \Rightarrow t

So, This Condition is False.

(iii) $|XY| \leq P$

We have to add x and y string character.

$$x + y = 8$$

$$\therefore |XY| = 8 \neq P, P = 7$$

So, This Condition is False.

Hence, $A = \{a^n b^n \mid n > 0\}$ is a NOT Regular Language.

Ex Prove that $A = \{yy \mid y \in \{0,1\}^*\}$ is not Regular.

\Rightarrow Here, Assume that A is a Regular Language and Pumping Lemma Length = $P = 7$

Here, $S = 0^P 1 0^P 1$ or $0 1^P 0 1^P$

We take $S = 0^P 1 0^P 1$

$$\therefore S = 0^7 1 0^7 1$$

We have to divide this S string into three part

$$\begin{aligned} \therefore X &= 00 \\ Y &= 0000 \\ Z &= 01000000001 \end{aligned}$$

We have to check Three Pumping Lemma Condition.

(i) $X \neq \epsilon$

Here, String X, Y and Z is part of A Regular Language.

(ii) $|Y| > 0$

Here, We have to take y^i and compare with strings.

Here, We take $y = Z$

$$\therefore XY^2Z = 0000000000000100000001$$

$$\therefore XYZ = 0000000100000001$$

$$\therefore XYZ \neq XY^2Z$$

So, This Condition is False

So, This condition is False

(iii) $|XY| \leq P$

We have to add x and y string character.

$$x + y = 8$$

$$\therefore |XY| = 8 \neq P, \quad P = 7$$

So, This condition is False.

Hence, $A = \{a^n b^n \mid n > 0\}$ is a NOT Regular Language.

Ex Prove that $A = \{yy \mid y \in \{0,1\}^*\}$ is not Regular.

\Rightarrow Here, Assume that A is a Regular Language and Pumping Lemma Length = $P = 7$

Here, $S = 0^P 1 0^P 1$ or $0 1^P 0 1^P$

We take $S = 0^P 1 0^P 1$

$$\therefore S = 0^7 1 0^7 1$$

We have to divide this S string into three part.

$$\begin{aligned} \therefore X &= 00 \\ Y &= 0000 \\ Z &= 0100000001 \end{aligned}$$

We have to check Three Pumping Lemma Condition.

(i) $X \neq \emptyset$

Here, String X, Y and Z is part of A Regular Language.

(ii) $|Y| > 0$

Here, we have to take y^i and compare with strings.

Here, we take $y = 2$

$$\therefore XY^2Z = 000000000000100000001$$

$$\therefore XYZ = 0000000100000001$$

$$\therefore XYZ \neq XY^2Z$$

So, This Condition is False.

(iii) $|xy| \leq p$

We have to add x and y string character

$$x + y = 6$$

$$\therefore |6| \leq 7$$

This condition is True.

For Pumping Lemma Not Regular Language all the condition is must be true.

Hence, $A = \{xyx \mid y \in \{0, 1\}^* \}$ is Not Regular Language.